

UNIVERSITY OF CALICUT
SCHOOL OF DISTANCE EDUCATION
B Sc. Mathematics (2011 Admission Onwards)
II SEMESTER
Complementary Course

PROBABILITY DISTRIBUTIONS (STATISTICS)

QUESTION BANK

1. The joint cumulative distribution function $F(x,y)$ lies within the values
 - a). -1 and +1
 - b). -1 and 0
 - c). $-\infty$ and 0
 - d). 0 and 1
2. If x and y are two independent random variables then $f(x,y) = \dots$
 - a). $f(x)+f(y)$
 - b). $f(x)-f(y)$
 - c). $f(x).f(y)$
 - d). $f(x)/f(y)$
3. The value of $F(-\infty+\infty) = \dots$
 - a). 0
 - b). 1
 - c). $+\infty$
 - d). $-\infty$
4. If X and Y are two independent r.v.'s the cumulative distribution function $F(x,y)$ is equal to
 - a). $F_1(x).F_2(y)$
 - b). $P(X \leq x, Y \leq y)$
 - c). both a and b
 - d). neither a nor b
5. If X and Y are two independent r.v.'s then
 - a). $E(XY)=1$
 - b). $E(XY) = 0$
 - c). $E(XY)=E(X).E(Y)$
 - d). $E(XY) = \text{a constant}$
6. If X and Y are two random variables such that their expectations exist and $P(x \leq y)=1$ then
 - a). $E(X) \leq E(Y)$
 - b). $E(X) \geq E(Y)$
 - c). $E(X)=E(Y)$
 - d). None of the above
7. If X is a random variable then $E(X-E(X))^2 = \dots$
 - a). μ_1
 - b). μ_2
 - c). μ_3
 - d). μ_4
8. If X and Y are two random variables then
 - a). $E(XY)^2 = E(X^2).E(Y^2)$
 - b). $E(XY)^2 = E(X^2Y^2)$
 - c). $E(XY)^2 \geq E(X^2)E(Y^2)$
 - d). $E(XY)^2 \leq E(X^2)E(Y^2)$
9. If X and Y are two random variables then the expression $E(X-E(X))(Y-E(Y))$ is called:
 - a). $V(X)$
 - b). $V(Y)$
 - c). $\text{Cov}(X,Y)$
 - d). Correlation of X and Y
10. If X is a random variable with mean μ then $E(X-\mu)^r$ is called :
 - a). variance
 - b). r^{th} raw moment
 - c). r^{th} central moment
 - d). none of the above

11. If X is a r.v having pdf $f(x)$, then $E(X)$ is called
- Arithmetic mean
 - Geometric mean
 - Harmonic mean
 - First Quartile
12. If X is a r.v. and r is an integer, then $E(X^r)$ represents
- r^{th} central moment
 - r^{th} raw moment
 - r^{th} factorial moment
 - none of these
13. For Bernoulli distribution with probability p of a success and q of a failure, the relation between mean and variance that holds is
- mean < variance
 - mean = variance
 - mean \geq variance
 - None of these
14. The mean and variance of a binomial distribution are 8 and 4 respectively. Then $P(X=1)$ is equal to
- $2^{\frac{1}{12}}$
 - $2^{\frac{1}{4}}$
 - $2^{\frac{1}{6}}$
 - $2^{\frac{1}{8}}$
15. If $X \sim B(n, p)$, $n = 4$ and also $P(X = 2) = 3P(X = 3)$, the value of p is
- 1
 - $\frac{1}{3}$
 - $\frac{9}{11}$
 - none of the above
16. If $f(x, y) = 4xy$; $0 < x < 1$, $0 < y < 1$, then $E(y/x) = \dots\dots$
- 4
 - 2
 - $\frac{4}{3}$
 - $\frac{2}{3}$
18. $E(Y / X = x)$ is called
- regression curve of x on y
 - regression curve of y on x
 - both a and b
 - neither a nor b
19. If $f(x, y) = 4xy$; $0 < x < 1$, $0 < y < 1$, the covariance between x and y is....
- $\frac{1}{48}$
 - $\frac{1}{144}$
 - $\frac{1}{4}$
 - None of these.
20. If X and Y are two independent r.v.s then $E(XY) = \dots\dots$
- $E(X) + E(Y)$
 - $E(X) - E(Y)$
 - $E(X).E(Y)$
 - None of these.
21. If X and Y are two r.v.s, the correlation coefficient between X and Y lies between
- 0 and 1
 - 1 and 0
 - 1 and 1
 - None of these.
22. If $X \sim B(n, p)$, mean = 4, variance = $4/3$, then $P(X = 5) = \dots\dots$
- $\left(\frac{2}{3}\right)^6$
 - $\left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)$
 - $\left(\frac{1}{3}\right)^6$
 - $4\left(\frac{2}{3}\right)^6$

46. Normal distribution was invented by
 a).Laplace c).Gauss
 b).De-Moivre d).All the above.
47. If X_1 and X_2 are two independent Poisson variates with parameters λ_1 and λ_2 respectively, then the variable $(X_1 + X_2)$ follows.
 a).Binomial distribution with parameters $(\lambda_1 + \lambda_2)$
 b).Poisson distribution with parameter $(\lambda_1 + \lambda_2)$
 c).Either of a and b
 d).Neither of a and b
48. The skewness of a binomial distribution will be zero if
 a). $p < \frac{1}{2}$ c). $p = \frac{1}{2}$
 b). $p > \frac{1}{2}$ d). $p < q$
49. Binomial distribution tends to Poisson distribution when
 a). $n \rightarrow \infty$, $p \rightarrow 0$ and $np = \lambda$ (finite)
 b). $n \rightarrow \infty$, $p \rightarrow \frac{1}{2}$ and $\lambda = \lambda$ (finite)
 c). $n \rightarrow 0$, $p \rightarrow 0$ and $np \rightarrow 0$
 d). $n \rightarrow 0$, $p \rightarrow 0$ and $np \rightarrow -\infty$
50. A discrete random variable has pmf $p(x) = kq^x p$; $p + q = 1$; $x = 2, 3, 4, \dots$
 The value of k is
 a). $\frac{1}{q^2}$ c). $\frac{1}{q}$
 b). $\frac{1}{p}$ d). $\frac{1}{pq}$
51. If a discrete random variable takes on four values -1,0,3,4 with probabilities $\frac{1}{6}, k, \frac{1}{4}$ and $1-6k$, where k is a constant. The value of k is
 a). $\frac{1}{3}$ c). $\frac{1}{12}$
 b). $\frac{2}{9}$ d). $\frac{5}{24}$
52. Let X be a continuous random variable with probability density function is
 $f(x) = kx$; $0 \leq x \leq 1$ = k ; $1 \leq x \leq 2$
 = 0; otherwise.
 The value of k is equal to
 a). $\frac{1}{4}$ c). $\frac{2}{5}$ b). $\frac{2}{3}$ d). $\frac{5}{4}$
53. For the distribution function of a random variable X, $F(5) - F(2)$ is equal to
 a). $P(2 < x < 5)$ c). $P(2 \leq x \leq 5)$
 b). $P(2 \leq x < 5)$ d). $P(2 < x \leq 5)$
54. If a continuous random variable X has probability density function,
 $f(x) = \frac{1}{3}$; $1 \leq x \leq 2$ = $\frac{2}{3}$; $0 \leq x \leq 1$ then $E(X^2)$ is equal to
 a). $\frac{1}{9}$ b). $\frac{2}{3}$ c). $\frac{5}{12}$ d). $\frac{1}{3}$
55. If binomial random variable has mean=4 and variance = 3, then its third central moment μ_3 is
 a). $\frac{1}{2}$ b). $\frac{5}{2}$ c). $\frac{3}{2}$ d). $\frac{7}{4}$
56. A poisson random variable has $\mu_4 = 2$ the value of its mean is
 a). $\frac{1}{3}$ b). $\frac{2}{3}$ c). $\frac{1}{4}$ d). $\frac{3}{4}$
57. A random variable has uniform distribution over the interval $[-1,3]$.
 This distribution has variance equal to
 a). $\frac{8}{5}$ b). $\frac{4}{3}$ c). $\frac{13}{4}$ d). $\frac{9}{2}$

70. If a bivariate normal distribution with parameter $(\mu_x, \mu_y, \sigma_x^2, \sigma_y^2, \rho)$ such that $\sigma_x = \sigma_y, \rho = 0$, the distribution is known as
- Uniform normal
 - Rectangular normal
 - Elliptical normal
 - Circular normal
71. If in a bivariate normal distribution with parameter $(\mu_x, \mu_y, \sigma_x^2, \sigma_y^2, \rho)$ such that $\sigma_x \neq \sigma_y, \rho = 0$, the distribution is named as
- symmetrical normal
 - uniform normal
 - elliptical normal
 - circular normal
72. If in a bivariate normal distribution of the variables x and y , $\rho_{xy} = 0$, it implies that x and y are
- Uncorrelated but not independent
 - Uncorrelated and independent
 - Independent but not uncorrelated
 - Correlated and dependent
73. Bivariate normal distribution is also named as
- Bravais distribution
 - Laplace-Gauss distribution
 - Gaussian distribution
 - All the above
74. Joint distribution function of (X, Y) is equivalent to the probability
- $P(X = x, Y = y)$
 - $P(X \leq x, Y \leq y)$
 - $P(X \leq x, Y = y)$
 - $P(X \geq x, Y \geq y)$
75. For the joint pdf $f(x, y)$, the marginal distribution of Y given $X=x$ is given as
- $\sum_{all\ x} f(x, y)$
 - $\int_{-\infty}^{\infty} f(x, y) dx$
 - $\int_{-\infty}^{\infty} f(x, y) dy$
 - $\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) dx dy$
76. If X and Y are independent, the cumulative distribution $F_{XY}(x, y)$ is equal to
- $F_X(x)F_Y(y)$
 - $P(X \leq x)P(Y \leq y)$
 - both a and b
 - neither a nor b
77. If the joint distribution of the variables X and Y is bivariate normal (BVN) $(0, 0, 1, 1, \rho)$, the correlation coefficient between X^2 and Y^2 is equal to
- 1
 - 1
 - ρ^2
 - 0
78. The correlation coefficient ρ between two variables X_1 and X_2 for a bivariate population in terms of moments is
- $\frac{\mu_{22}}{\sqrt{\mu_{20}\mu_{02}}}$
 - $\frac{\mu_{11}}{\sqrt{\mu_{20}\mu_{02}}}$
 - $\frac{\mu_{12}}{\sqrt{\mu_{11}\mu_{22}}}$
 - $\frac{\mu_{12}}{\sqrt{\mu_{20}\mu_{02}}}$
79. The conditional distribution of a discrete variable Y given $X=x$ can be expressed as
- $F_{Y/x}(y/x) = P(Y \leq y/X = x)$
 - $F_{Y/x}(y/x) = P(Y = y/X = x)$
 - $F_{Y/x}(y/x) = \frac{P(Y \leq y/X \leq x)}{P(X=x)}$
 - $F_{Y/x}(y/x) = \frac{P(X=x/Y=y)}{P(X=x)}$
80. The conditional pdf of X given $Y=y$ for a joint density $f_{X,Y}(x, y)$ can be found by the formula
- $F_{X/y}(x/y) = \frac{f_{X,Y}(x,y)}{f_X(x)}$
 - $F_{X/y}(x/y) = F_{Y/x}(y) \cdot f_{X,Y}(x,y)$
 - $F_{X/y}(x/y) = \frac{f_{X,Y}(x,y)}{f_Y(y)}$
 - None of the above.

99. If $Var(x) = 1$, then $Var(2X \pm 3)$ is
 a).5 b).13 c).4 d).2
100. $E(X - k)^2$ is minimum when
 a). $k < E(X)$ c). $k = E(X)$
 b). $k > E(X)$ d). $k = 0$
101. Let X and Y be two bivariate continuous random variables and $f(x,y)$ be its probability density function. Then random variables x and y are independent if $f(x,y) = f(x) \cdot f(y)$. Here $f(x)$ denote
 a) Values of function 'f' at 'x' c) $\int_x f(x,y)dx$
 b) $\int_y f(x,y)dy$ d) $\int_x \int_y f(x,y)dx dy$
102. Two fair dice are tossed. Let x denote the difference (absolute) of 2 face numbers and y their sum. Then $P(x=2, y=7)$ is
 a) $\frac{1}{36}$ c) 0
 b) $\frac{2}{36}$ d) $\frac{5}{36}$
103. Two perfect dice are thrown simultaneously, If x = face number of the first dice and y that on the 2nd dice, which of the following is zero?
 a) $P(x=1, y=1)$ c) $P(x=2, y>3)$
 b) $P(x+y =1)$ d) $P(x=y)$
104. Following table gives the joint probability distribution of (x, y)

$\begin{matrix} x \\ y \end{matrix}$	1	2	3	4	P(y)
1	$\frac{1}{30}$	$\frac{1}{30}$	$\frac{2}{30}$	$\frac{1}{30}$	$\frac{5}{30}$
2	$\frac{2}{30}$	$\frac{2}{30}$	$\frac{4}{30}$	$\frac{2}{30}$	$\frac{10}{30}$
3	$\frac{3}{30}$	$\frac{3}{30}$	$\frac{6}{30}$	$\frac{3}{30}$	$\frac{15}{30}$
P(x)	$\frac{6}{30}$	$\frac{6}{30}$	$\frac{12}{30}$	$\frac{6}{30}$	1

- Then the marginal probability distribution at $y = 3$ is
 a) $\frac{6}{30}$ c) $\frac{12}{30}$
 b) $\frac{10}{30}$ d) $\frac{15}{30}$
105. If $f(x,y) = \frac{1}{8}(6-x-y), 0 < x < 2, 2 < y < 4 = 0$, other wise
 Then marginal probability of x is
 a) $\frac{1}{4}(5-y)$ c) $\frac{1}{4}(3-x)$
 b) $\frac{1}{3}(4-x)$ d) $\frac{1}{5}(4-y)$
106. If $f(x,y) = 2, 0 < x < y < 1 = 0$, otherwise, then the marginal probability density function of y is.
 a) 2, $0 < x < y$ c) 0
 b) $2y; 0 < y < 1$ d) 1

117. Consider the following table

	X		
		0	1
Y	-1	$\frac{1}{8}$	$\frac{2}{8}$
	1	$\frac{3}{8}$	$\frac{2}{8}$

- a) $\frac{4}{8}$ b) $\frac{2}{8}$ c) $\frac{-3}{8}$ d) $\frac{5}{8}$

118. Variance of x is given by

- a) $E(x - E(x))$ c) $E(x^2) - [E(x)]^2$
 b) $E(x^2) - E(x)$ d) $E(x^2)$

119. The distribution of a random variable x which takes 2 values 0 and 1 with respective probabilities q and p such that $(p+q)=1$ is called.

- a) Bernoulli Distribution c) All of these
 b) Binomial distribution d) None of these

120. For a binomial distribution $P(x) = nC_x \cdot P^x \cdot q^{n-x}$, $x = 0, 1, 2, \dots, n$, which of the following is incorrect?

- a) $\mu_1 = np$ c) $\mu_2 = np$
 b) $\mu_2 = n(n-1) p^2 + np$ d) $\mu_1 = 0$

121. The measure of skewness β_1 is related to the central moments as

- a) $\beta_1 = \frac{\mu_3}{\mu_2}$ c) $\beta_1 = \frac{\mu_3^2}{\mu_2^3}$
 b) $\beta_1 = \frac{\mu_2}{\mu_3}$ d) $\beta_1 = \frac{\mu_2^3}{\mu_3^2}$

122. A curve is said to be lipokurtic if

- a) $\frac{\mu_4}{(\mu_2)^2} - 3 > 0$ c) $\frac{\mu_4}{(\mu_2)^2} - 3 = 0$
 b) $\frac{\mu_4}{(\mu_2)^2} - 3 < 0$ d) None of these

123. Given mean and variance of binomial distribution is 4 & 3 respectively.

Then its mode is

- a) 3 c) None of these
 b) 4 d) Cannot be found

124. The Poisson's distribution is a limiting case of the binomial distribution under the following conditions, except one. Which one?

- a) Number of trials is indefinitely large.
 b) Probability of success is indefinitely large
 c) $np = \lambda$
 d) Probability of failure is indefinitely large

125. A random variable is said to be Poisson variate if it assumes non-negative values and its probability mass function is given by $P(x) =$

- a) $\frac{e^{-\lambda} \cdot \lambda^x}{x!}, x = 0, 1, 2, \dots, \infty$ c) $\frac{e^{-\lambda} \cdot \lambda^{-x}}{x!}, x = 0, 1, 2, \dots, \infty$
 b) $\frac{e^{-\lambda} \cdot \lambda^x}{x!}, x = 0, 1, 2, \dots, \infty$ d) $\frac{e^{-\lambda}}{\lambda^{-x} x!}, x = 0, 1, 2, \dots, \infty$

126. If x is a Poisson variate with $P(x=2) = 9 \times P(x=4) + 90 \times P(x=6)$, then mean =
 a) 1 b) 2 c) 3 d) -1
127. For a Poisson distribution having a double mode at $x=1$ and $x=2$, what is $P(x=3)$?
 a) $\frac{4e^{-2}}{3}$ b) $\frac{4e^2}{3}$ c) $\frac{3e^2}{4}$ d) $\frac{3e^{-2}}{4}$
128. x and y be independent Poisson variate such that $P(x=0) = P(x=2)$ & $P(y=1) = P(y=2)$. Then $V(x - y) =$
 a) $\sqrt{2} - 2$ b) $2 - \sqrt{2}$ c) $\sqrt{2} - 2$ d) $\sqrt{2} + 2$
129. A continuous random variable follows a standard normal distribution if its pdf is given by
 a) $f(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2}, -\infty < z < \infty$ b) $f(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2}, -\infty < z < \infty$
 c) $\frac{1}{2\pi} e^{-z^2/2}, -\infty < z < \infty$ d) $\frac{1}{\sqrt{2\pi}} e^{-z/2}, -\infty < z < \infty$
130. The binomial distribution has number of parameters equal to _____
 a) two b) one c) four d) three
131. The binomial distribution have mean equal to
 a) $\mu = p$ b) $\mu = npq$ c) $\mu = np$ d) None of these
132. In Binomial distribution the variance σ^2 and mean μ are related by
 a) $\sigma^2 = q\mu$ b) $\sigma^2 = \frac{\mu}{q}$ c) $q^2\sigma^2 = \mu$ d) None of these
133. The range of the Bernoulli random variable is the set
 a) Set of real members b) (0, 1)
 c) Set of integers d) None of these
134. Let $\phi(x)$ be a standard normal distribution function. Then the following relation holds.
 a) $\phi(-x) = \phi(x)$ b) $\phi(-x) = \phi(x) - 1$
 c) $\phi(-x) = 1 - \phi(x)$ d) $\phi(-x) = \phi(x) + 1$
135. The variance of the uniform (discrete) probability distribution is given by
 a) $\sum \frac{(x - \mu)^2}{k^2}$ b) $\sum \frac{x_i}{k}$ c) $\sum x_i$ d) k
136. We get standard normal distribution from normal distribution if
 a) $\mu = 1, \sigma = 0$ c) $\mu = \sigma = 0$
 b) $\mu = 0, \sigma = 1$ d) $\mu = \sigma = 1$
137. Let $F(x)$ be a distribution function of normal distribution and $\phi(x)$ be a standard distribution function. Then the following relation holds.....
 a) $F(x) = \phi\left(\frac{x}{\sigma}\right)$ b) $F(x) = \phi(x)$
 c) $F(x) = \phi(\sigma)$ d) $F(x) = \phi\left(\frac{x - \mu}{\sigma}\right)$

138. Repeated trials are normally referred to _____
- a) Gamma distribution
 - b) Uniform distribution
 - c) Bernoulli distribution
 - d) None of these
139. The mean and variance of Poisson distribution are same
- a) Always true
 - b) Always false
 - c) Partially true
 - d) Partially false
140. When each term of the given series may assume the values of two or more than two variables, the distribution is called
- a) Variate
 - b) Non variate
 - c) Univariate
 - d) Bivariate
141. If x is a random variable with $E(x) = \mu$ and $V(x) = \sigma^2$ then Chebyshev's inequality is given by
- a) $P[|x - \mu| \geq k\sigma] \leq \frac{1}{k^2}, k > 0$
 - b) $P[|x - \mu| \leq k\sigma] \geq 1 - \frac{1}{k^2}, k > 0$
 - c) Both a and b
 - d) None of these

ANSWERS

1.d	37.d	73.d	109. a
2. c	38.d	74.b	110. c
3.b	39.c	75.b	111.d
4.b	40.a	76.c	112.a
5.c	41.b	77.c	113.c
6.a	42.b	78.c	114. b
7.b	43.b	79.c	115.a
8.d	44.d	80.c	116.c
9.c	45.d	81.c	117.a
10.c	46.c	82.b	118.c
11.a	47.b	83.b	119.a
12.b	48.c	84.d	120. c
13.a	49.a	85.b	121. c
14.a	50.a	86.c	122.a
15.c	51.c	87.d	123. b
16.d	52.b	88.a	124. b
17.c	53.c	89.b	125.d
18.b	54.d	90.d	126. a
19.d	55.c	91.a	127. a
20.c	56.b	92.d	128.d
21.c	57.b	93.a	129.b
22.b	58.d	94.a	130.a
23.b	59.d	95.c	131.c
24.d	60.c	96.c	132. a
25.d	61.b	97.b	133. b
26.d	62.c	98.b	134. c
27.b	63.a	99.c	135. a
28.d	64.c	100.c	136. b
29.a	65.b	101. b	137. d
30.a	66.c	102. c	138. c
31.c	67.a	103. b	139. a
32.b	68.b	104. d	140. d
33.a	69.a	105. c	141. c
34.c	70.d	106.b	
35.c	71.c	107. b	
36.b	72.b	108. d	

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